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PARAMETERIZATION OF TERRAIN IN ARMY COMBAT ANALYSIS

Christopher James Needels

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NAVAL POSTGRADUATE SCHOOL Monterey, California



THESIS

PARAMETERIZATION OF TERRAIN
IN ARMY COMBAT ANALYSIS

Christopher James Needels

March | 976

Thesis Advisor:

Samuel H. Parry

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SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
Parameterization of Terrain in Army Combat Analysis		5. TYPE OF REPORT & PERIOD COVERED Master's Thesis; March 1976 6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(*) Christopher James Needels		8. CONTRACT OR GRANT NUMBER(a)
9. PERFORMING ORGANIZATION NAME AND ADDRESS Naval Postgraduate School Monterey, California 93940		10. PROGRAM ÉLEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
Naval Postgraduate School Monterey, California 93940		March 1976 13. NUMBER OF PAGES 87
Naval Postgraduate School Monterey, California 93940	from Controlling Office)	15. SECURITY CLASS. (of this report) Unclassified 15a. DECLASSIFICATION/DOWNGRADING SCHEDULE

16. DISTRIBUTION STATEMENT (of this Report)

Approved for public release; distribution unlimited

17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, If different from Report)

18. SUPPLEMENTARY NOTES

19. KEY WORDS (Continue on reverse side if necessary and identify by block number)

- 1. Terrain Modelling
- 2. SIMTER (Simulated Terrain Model)

20. ABSTRACT (Continue on reverse side if necessary and identify by block number)

This study presents and evaluates a methodology for parameterizing terrain for use in land combat analysis. The current procedure is to use digitized data which is compiled from actual terrain by engineer surveys and photo-interpretation. However, for those studies which do not require exact representation of terrain, a less costly and time consuming method can be used. In particular, terrain can be created

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mathematically by using a modified bivariate normal probability density function. An additional advantage of this approach is that the macro-terrain features can be created at random, thereby providing multiple, unique realizations of a type of terrain. This capability overcomes the sensitivity of Army study results to a single sample of terrain. When used for line-of-sight calculations, the parameterized, continuous representation eliminates the need for interpolations required for digitized terrain. The methodology and simulation can be employed independently or used as a preprocessor for other combat models.

Parameterization Of Terrain in Army Combat Analysis

by

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Major, United States Army
B.S., United States Military Academy, 1965

Submitted in partial fulfillment of the requirement for the degree of

MASTER OF SCIENCE IN OPERATIONS RESEARCH

from the
NAVAL POSTGRADUATE SCHOOL
March 1976

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I. INTRODUCTION

The representation of terrain in many Army combat simulation models is both costly and time consuming. instance, terrain input for high resolution models such as Dynamic Tactical Simulation (DYNTACS), Tank Exchange Model (TXM), and various versions of the Bonder/Individual Unit Action model comes from computer tapes prepared ρA as the Army Map Service and the Waterways Experiment Station. These tapes typically contain terrain ten meter intervals for an entire piece of actual terrain. To survey and record the 18,000 grid intersections for a six kilometer by three kilometer section of terrain is expensive and, as is suggested by this paper, unnecessary many applications. The storage of this information not only can require a major portion of a computers storage capacity (core), but also require a great deal of running time searching this stored data in order to make movement line-of-sight calculations. The exact amount of core and running time depends upon the type computer, the resolution of the model, and the dimensions of the selected peice of terrain.

method of terrain representation is also The current statistically questionable. Vector Research, In a Incorporated (VRI) study on terrain line-of-sight, past Army study results, concluded that "...present and based on the analysis of combat results on a very limited sample of terrains, may have been determined by the terrain selection process and not by the actual weapon system or force design differences." More specifically it stated the following:

a. "There is extreme sensitivty in combat model results as the scenarios (terrain and movement assumptions) are varied, even when variation is within a class of scenarios chosen for their "a priori" equivalence.

b. "This sensitivity can be slightly reduced, but remains extreme (with probabilities of win estimable only within plus or minus 25%) even when battle results are used to redesign scenarios."

These results imply that sufficient replications of each type of terrain should be run in order to reach a satisfactory statistical level of significance. For VRI's analysis at least 50 replications of each type of terrain were used.

The problems stated above suggest that new methodology for the representation of terrain is necessary in order to reduce costs, shorten computer running time, and improve the level of significance for Army studies which use combat models. Consequently, the objective of this paper is to develop this new technology using parameterized, randomly created terrain, and to verify the concepts using a computerized terrain simulation model.

Investigations of the Variation of Combat Model Predictions With Terrain Line of Sight, p. 7, Vector Research, Incorporated, 1975.

2. Ibid., p. 6.
3. Ibid., p. 5.

II. TERRAIN REPRESENTATION

A. STATE OF THE ART

DYNTACS, which is one of the most frequently used high resolution combat simulations, serves as a good example of the state of the art in terrain representation and use. general terms DYNTACS is a two-sided, dynamic, Monte Carlo, highly interactive combat simulation capable of representing from a single crew served weapon to a reinforced In particular the model considers in detail effects of terrain on detection, mobility, tactics, and intervisibility between weapon elements. For the remainder of this paper, unless otherwise specified. macro-terrain (elevation and slope) will be considered. previously mentioned this data is supplied by the Waterways Experiment Station (WES) on computer tapes. Although these tapes have a ten meter resolution, DYNTACS is generally run using 100 meter squares. The simulation divides each grid square diagonally, thus producing a series of adjoining triangular terrains. The entire battlefield, therefore, a surface of equally sized triangles which represented as vary in slope depending upon the elevation at their corners.

From the macro-terrain data, line-of-sight between any two opposing elements is computed. This is accomplished by first computing an angle between the horizontal and a straight line drawn between an observer and target (0-T The program then conducts a search of the terrain along the path of the O-I line to see if any macro-terrain is higher than the O-T line itself. This is accomplished by comparing the angle of the O-T line with the angle horizontal of the observer-terrain line. If the latter angle is larger, there is no intervisibility. Over the duration of a battle with numerous elements this calculation may be made thousands of times. Consequently, not only is the time to prepare the tapes high, but also the time to compute lines-of-sight once the terrain is input to the model. Considerable effort by developers and users of this model has been expended to streamline this subroutine.

B. A DIFFERENT APPROACH

If a combat simulation is to be used for determining who will win a battle over a specific piece of ground such as the Fulda Gap, then that terrain should be modelled with precision. However, if the model is to be used to determine weapons effectiveness, then representation of a specific terrain is not necessary, and need only be representative of the area to be modelled. Furthermore, as VRI suggested, a single realization (e.g. the Fulda Gap) may produce inaccurate conclusions in a weapons system evaluation. is needed, therefore, is random terrain representation which can be replicated quickly. However, at the same time must be representative of a particular "type" of terrain. One approach is to represent hills precisely using a series mathematical equations. This method would eliminate the inaccuracies of digitized (discrete) terrain but would still have the problem of producing results based on a single realization of terrain. Moreover, the time involved to model with precision would negate its contribution. At the other end of the terrain modelling spectrum is to use cylinders or cones to represent hills. This is mathematically appealing, but lacks realism even if the were proven statistically satisfactory. solution, therefore, lies somewhere in between.

An equation that produces what appears to be a simple hill and at the same time is mathematically tractable is the bivariate normal probability density function. Figure 1 is a sample realization of terrain created and drawn by a computer, using the bivariate normal distribution. The second figure is a contour map of the same terrain, also drawn by the computer.

TERRAIN

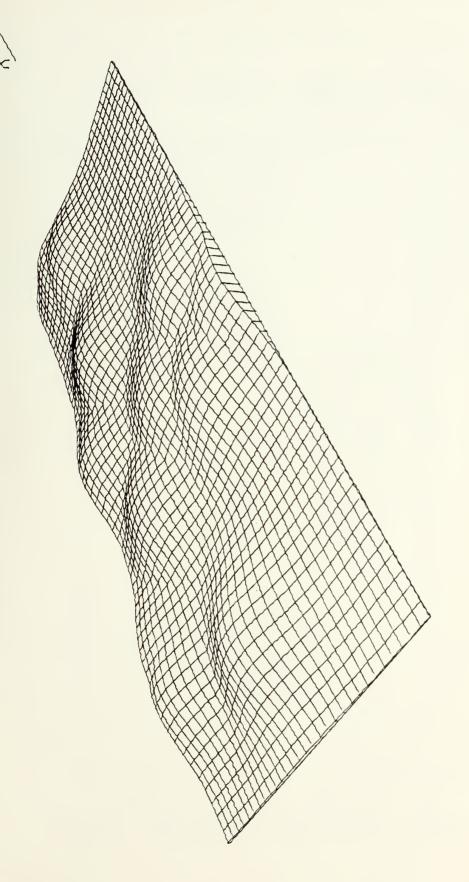


Figure 1: Sample of Computer Created Terrain

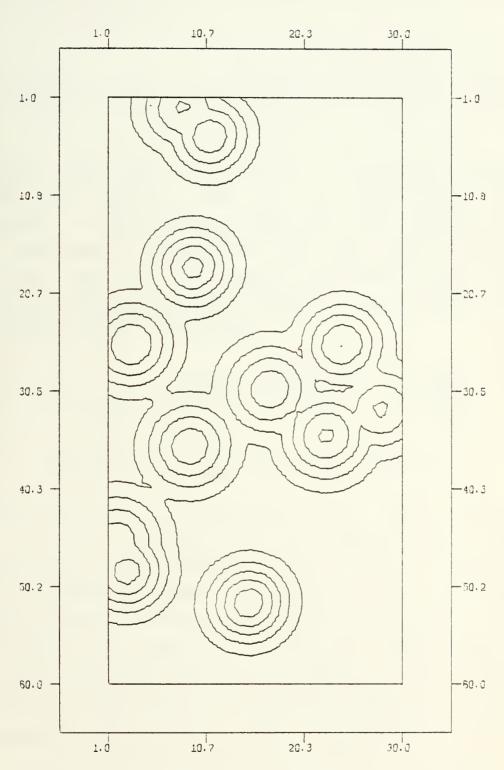


Figure 2: The Sample Depicted as a Contour Map

The common form of the bivariate normal (BVN) density function is as follows:

$$f(x,y) = \frac{1}{2 \pi \sigma_{x} \sigma_{y}(1-\rho^{2})} \exp \left\{ -\frac{1}{2 (1-\rho^{2})} \left[\left(\frac{x-\mu_{x}}{\sigma_{x}} \right)^{2} - 2\rho \frac{(x-\mu_{x})(y-\mu_{y})}{\sigma_{x} \sigma_{y}} + \left(\frac{y-\mu_{y}}{\sigma_{y}} \right)^{2} \right] \right\}$$

Since this equation is that of a probability density function, its integral over $(-\infty, +\infty)$ must equal 1.0. Consequently, as the standard deviations are increased, the hill is flattened. Additionally, even with small standard deviations, the hill will remain less than one unit high. Therefore, to be useful to the modeller, the equation has been modified (MBVN) as follows:

$$(1.2) \quad Z=C \quad exp\left\{-\frac{1}{2(1-\rho^2)}\left[\begin{pmatrix}x-\mu_x\\---\\\sigma_x\end{pmatrix}^2-2\rho\begin{pmatrix}x-\mu_x\\---\\\sigma_y\end{pmatrix}(y-\mu_y)+\begin{pmatrix}y-\mu_y\\---\\\sigma_y\end{pmatrix}^2\right]\right\}$$

where C is the peak elevation of the hill.

There are two major advatages of the MBVN equation. First, it is appealing to an observer as a good representation of many different types of hills. Secondly, it has a sufficient number of parameters to vary the shape of a hill without becoming mathematically intractable. The parameters $\sigma_{\rm X}$, $\sigma_{\rm Y}$, and ρ control the shape in the XY plane, the C parameter controls the height of the hills, and $\mathcal{M}_{\rm X}$ and $\mathcal{M}_{\rm Y}$ determine the location of the center of the hill on its map. (See Figure 3 for illustrations of the parameters).

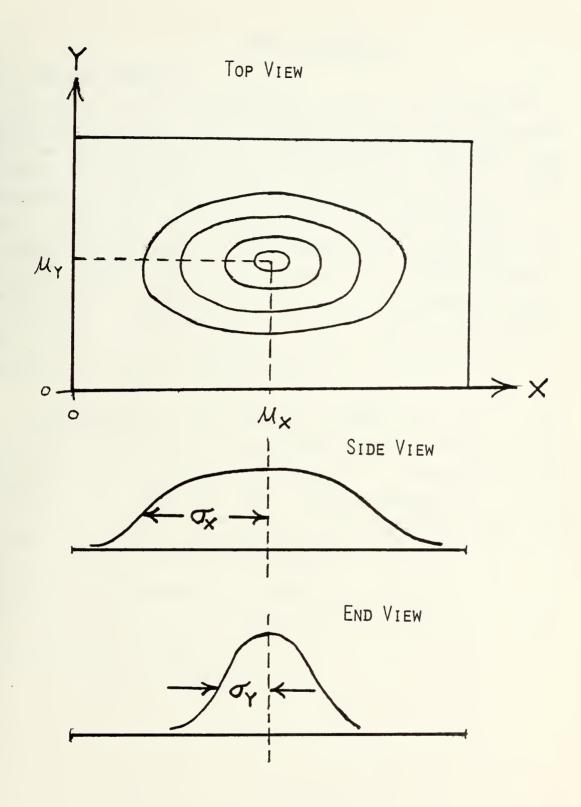


FIGURE 3: SINGLE HILL PARAMETERS

III. MODEL METHODOLGY

A. TERRAIN SIMULATOR

So far in the discussion of the new approach to modelling terrain, only a single hill has been discussed. This has been important as a mathematical foundation, but lacking in practical value. To be of use in a combat simulation, the hills must be created collectively in a size, quantity, and configuration so as to represent a desired type of terrain. For example, a user may want terrain characterized by a few, low rolling hills; or perhaps rugged, mountains with peaks of widely varying elevations. Both can be modelled by adjusting parameters. The remainder of this chapter explains the methodology by examining a working terrain model.

The Simulated Terrain Model (SIMTER) has two parts. The first is the main program which creates terrain and, at the discretion of the user, plots both a three-dimensional drawing and a contour map. Used strictly for terrain generation, it can be used as a preprocessor for other combat models by producing grid points and elevations similar to those provided on computer tapes by WES. The second part of SIMTER is a movement/line-of-sight subroutine (MOVLOS) which moves a target along specified routes across the generated terrain. This part will be discussed in further detail in Chapter V.

In addition to those input parameters used to describe a single hill, others are used to aggregate the hills into a map. These include the following:

- 1. The dimensions of the battlefield in meters.
- 2. The grid interval (e.g. 10 meters or 100 meters).
- 3. The number of hills to be created.
- 4. How much the peaks of the hills are to vary.
- 5. How much the spread of the hills are to vary.
- 6. How many ridge lines, if any, are to be created.

Given the input parameters, the model proceeds as follows.

- 1. The first step of the program is to randomly select the centers of mass for the desired number of hills. This operation is performed by drawing Uniform (0,1) random numbers and multiplying them by the size of the battlefield in the X and Y directions, thus producing an array of paired grid points. If ridge line are desired, then the random points in either the X or Y direction, but not both, can be biased by drawing random normal deviates about a preselected ridgeline center. Although not a requirement, this particular program makes a hasty plot of the centers of mass points for visual reference of the random process.
- 2. The second step is to create the dimensions of each MBVN hill. If the user desires that all the hills be of the same size and shape then this step is complete. However, for most cases the height and spread of each hill will be varied according to an input parameter which is actually the standard deviation for the variations. For example, if a user desires hills which average 100 meters high, but vary about this average value by approximately 30 meters, then 100 becomes the mean value for the peaks of the hills which vary in individual elevations according to normally distributed random numbers whose standard deviation is 30.

The same procedure is done for the spread of the hills in both the X and Y directions.

If only movement and line-of-sight calculations are to be made, then MOVLOS subroutine is called and the program is terminated. A major advantage of this approach to terrain modelling is that no 10 meter, 100 meter, or other grid system is necessary. The terrain representation is continuous; therefore, the elevation at any point on the map can be found without storing any digitized (discrete) map information. Only the hill parameters need be stored.

3. If a matrix of grid values is desirable, as would be the case if the program were used in lieu of the WES computer tapes, then the third part of the SIMTER main program is the creation of an evenly spaced grid system, to include the elevation at each grid line intersection. For all the maps and drawings in this study, a 100 meter grid interval was used.

Since the BVN distribution has some finite value (elevation) in all directions, regardless of how far removed from its center, the elevation of each hill must be computed for each point in the grid system. As each hill is checked for its elevation at any selected point, it is compared with its predecessor. If it is lower, it is discarded; otherwise it is saved for comparison with the next hill's elevation at that same point. After each hill has been searched, only the highest value is stored. It is this value, along with the other maximum values at each grid interval, which make up the terrain surface. If there is a large number of hills, the search process can be streamlined by truncating the MBVN if the height of the density falls below some specified value.

4. The final part of the program is to provide the desired output. This particular program provides both printed and

graphical cutput. Both the contour map and the three-dimensional drawing were produced by a California Computers Compay CALCOMP Plotter.

B. USER INTERFACE

To be of value to the user, the model must be flexible and its results realistic. In order to demonstrate these capabilities numerous test runs were conducted. The first group of runs used three different average elevations (100, 200, and 300 meters) and three different numbers of hills (5,15,25). The nine resulting terrains are depicted Appendix A. All maps and drawings represent a 6,000 meter by 3,000 meter battlefield. The second group of runs displays the results of varying the seeds of the Uniform (0,1) random number generator which were used to create the hill centers (Appendis B). The third group (Appendix C) demonstrates the effects of changing the spreads of the hills. For all the tests listed above, the contour interval representing elevation was 50 meters.

IV. LINE-OF-SIGHT

A. THE PRECISE APPROACH

A major advantage of continuous terrain representation is that line-of-sight calculations can be made for any pair of grid coordinates. This is unlike discrete terrain which requires some approximate method such as linear interpolation. If a simple "yes" or "no" answer is desired for the question of intervisibility between any two points on the terrain surface then the mathematics consists of solving the simultaneous equations of a straight line (0-T line) and a curved surface in three space. If a solution exists then there is not line-of-sight, i.e. the line intersects the hills.

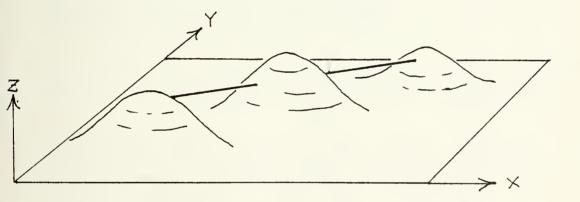


Figure 4: Line-of-Sight

The following is a summary of the procedures.

The O-T line is parameterized as follows:

$$(4.1) X = a + b t$$

$$(4.2)$$
 $Y = a_2 + b_2 t$

$$(4.3) Z = a_3 + b_3 t$$

The equations are then substituted into the MBVN equation, resulting in the following expression:

$$a_3+b_3t = C \exp \left\{-\frac{1}{2(1-\rho^2)} \left[\frac{a_1+b_1t-\mu_x}{\sigma_x} \right]^2 \right\}$$

One approach to solving this equation is to take natural logarithms of both sides, thus yielding

$$\ln(a_3+b_3t) = \ln C - \frac{1}{2(1-\rho^2)} \left[\begin{pmatrix} a_1+b_1t-\mu_x \\ -\sigma_x \end{pmatrix}^2 \right]$$

(4.5)
$$-2\rho - \frac{(a_1 + b_1 t - \mu_x)(a_2 + b_2 t - \mu_y)}{\sigma_x} + \left(\frac{a_2 + b_2 t - \mu_y}{\sigma_y}\right)^2$$

Expanding the left hand side using series expansion of a logarithm and truncating after three terms produces a quadratic expression. This can be combined with the quadratic on the right and solved using the standard quadratic formula. Unfortunately, the series has very poor convergence with only three terms. Using the average height of a hill as an approximate solution to the series, less than one decimal place accuracy can be expected. The expansion used is provided below:

(4.6)
$$\ln t = \ln a + \frac{(t-a)^2}{----} + \cdots 0 < t \le 2a$$

One approach to improving the accuracy of this solution is to solve the exact solution of a similar O-T line which is horizontal and a hill which is circular normal, and use the results to improve the convergence of the series in just three terms. An explanation of this approximation is provided in a later section.

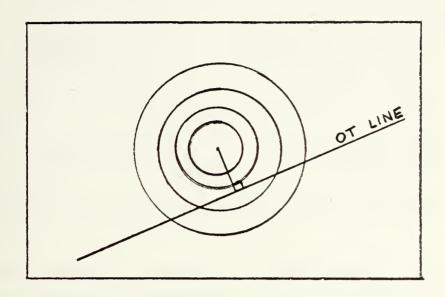
Another way of solving the problem of finding a sclution for the parameterized equations of a line and a surface is to use non-linear programming techniques. Using the rapid convergence properties of a Newton search near its solution, a precise answer can be found with minimal iterations.

B. AN APPROXIMATE APPROACH

If intervisibility lines (O-T lines) were horizontal and the MBVN hills were circular, then the mathematics would yield a quick, exact solution. This is done simlpy by projecting the O-T line onto the XY plane and finding the line from the center of the hill perpindicular to the O-T projection (See figure 5). The intersection of these two lines produces a set of coordinates in the XY plane. Finding the elevation of both the O-T line and the hill at this location yields two numbers which can be compared for line-of-sight. If the line is higher than the hill, then intervisibility exists.

Sample calculations to test the accuracy of this approximation yielded two decimal place precision for O-T lines less than 15 degrees from horizontal and MBVN hills whose spreads in the X and Y directions did not exceed ten per cent difference from each other. Fifteen degree angles can be exceeded in two general cases: very high hills and very close ranges. In other words the problem exists when the observer and target are at significantly different altitudes when close to each other. The inaccuracy is illustrated below. The curves represent two-dimensional cross sections of some part of a hill.

TOP VIEW



OBLIQUE VIEW

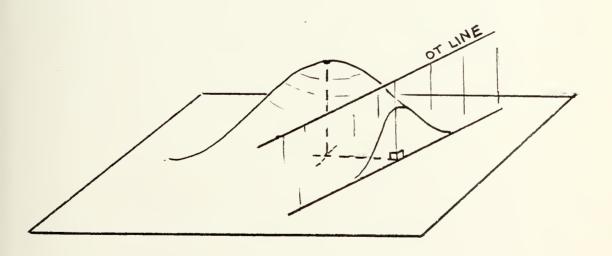


FIGURE 5: LINE-OF-SIGHT CALCULATION

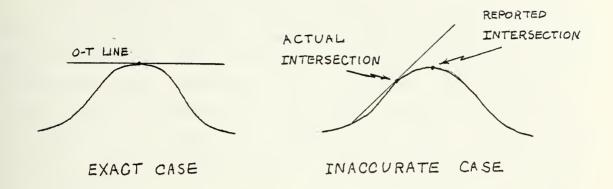


Figure 6: 0-T Line Intersection with Hill Cross Section

An efficient solution to the problem is to use the circular normal and horizontal line calculations as long as the situation remains within the confines listed above, and use a Newton search for those few cases which fall outside the desired accuracy.

V. MOVEMENT/LINE-OF-SIGHT SUBROUTINE

A. MODEL METODOLOGY

The movement/Line-of-sight subroutine (MOVLOS) performs three main calculations: movement, line-of-sight, and per cent of target area visible. To perform these functions additional input parameters are required. The first of these is the location of a stationary observer or defender, the second is an array of coordinates which depicts the route of a moving target, and the final input group includes the dimensions of the target. For this program the target is presumed to be rectangular so that height, width, and length are required.

general mathematics of the line-of-sight calculations were explained in Chapter IV. This section designed to explain the methodology of applying these mathematics to a combat model. The first step is determine the elevation of the observer by searching for the highest hill at the observer coordinates. accomplished by substituting the observer XY coordinates into the equation of each MBVN hill. The highest resulting functional value is the elevation of the observer. This procedure is likewise carried out for the elevation of the Using the three-dimensional coordinates of both the observer and the target, the subroutine forms the equations for the O-T line in three space. The projection of the O-T line onto the XY plane intersects at right angles with lines the centers of mass of each hill. coordinates of the intersections are used to determine the elevation of each hill along the O-T line by once again substituting into the MBVN equation of the respective hills.

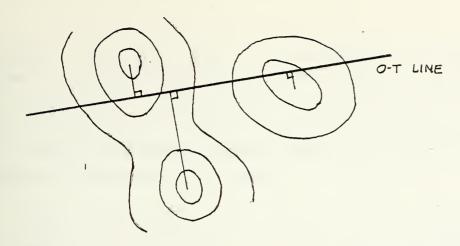


Figure 7: 0-T Line Projection

The elevation of the O-T line is also computed at each intersection. This is done using the ratio of sides of similar triangles.

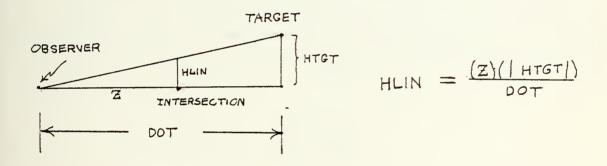


Figure 8: Height of O-T Line at Intersection

If any hill is higher than the O-T line along the line's path, then intervisibility does not exist.

To be of use in a high resolution model, the line-of-sight subroutine must answer more than "yes" or "no" to the question of intervisibility. Since the probability of a hit (P) is partly a function of target size, the program must determine what effective area of the target is visible to the firer. This, in turn, is a function of the target's dimensions, the per cent of area exposed above the

terrain, and the angle it is facing with respect to the observer. Using basic trigonmetry, MOVLOS computes the area of the target projected in the direction of the O-T line. Two possible target configurations are illustrated in Figure 9. The mirror images of these cases are calculated by using absolute values for the angles.

The dynamics of the program are provided by the movement portin of MOVLOS. At discrete time intervals, the target moves along the preselected routes toward its objective. For all runs of SIMTER a one-second time interval was used. At each second an instantaneous velocity and a line-of-sight are computed. If the velocity is not held constant, it is then solely a function of the slope of the terrain. The slope is found by taking the directional derivative (DEL) of the MBVN in the direction of the target. The directional derivative of f(x,y) in the direction is given by

For the Modified Bivariate Normal the partial derivatives are as follows:

$$\frac{\partial f}{\partial x} = \frac{C}{(1-\rho^2)} \begin{bmatrix} x-\mu_x & \rho y-\rho \mu_y \\ -\frac{\alpha}{2} & \sigma_x \end{bmatrix} exp \begin{cases} \frac{1}{2(1-\rho^2)} \begin{bmatrix} x-\mu_x \\ -\frac{\alpha}{2} \end{bmatrix} - \frac{\alpha}{2} \end{cases}$$

$$(5.2) \qquad 2\rho - \frac{(X - \mu_X)(Y - \mu_Y)}{\sigma_X \sigma_Y} + \left(\frac{Y - \mu_Y}{\sigma_Y}\right)^2$$

$$\frac{\partial f}{\partial y} = \frac{C}{(1-\rho^2)} \begin{bmatrix} Y-\mu_{Y} & \rho X-\rho \mu_{X} \\ -\frac{1}{2} & -\frac{1}{2} \\ \sigma_{Y} & \sigma_{X}\sigma_{Y} \end{bmatrix} exp \begin{cases} \frac{1}{2(1-\rho^2)} \begin{bmatrix} X-\mu_{X} \\ -\frac{1}{2} \\ \sigma_{X} \end{pmatrix}^{2} - \frac{1}{2(1-\rho^2)} \begin{bmatrix} X-\mu_{X} \\ -\frac{1}{2} \\ \sigma_{X} \end{bmatrix}^{2} \end{cases}$$

$$(5.3) \qquad 2\rho - - - \frac{(X - \mu_{X})(Y - \mu_{Y})}{\sigma_{X}\sigma_{Y}} + \begin{pmatrix} Y - \mu_{Y} \\ - - - \end{pmatrix}^{2}$$

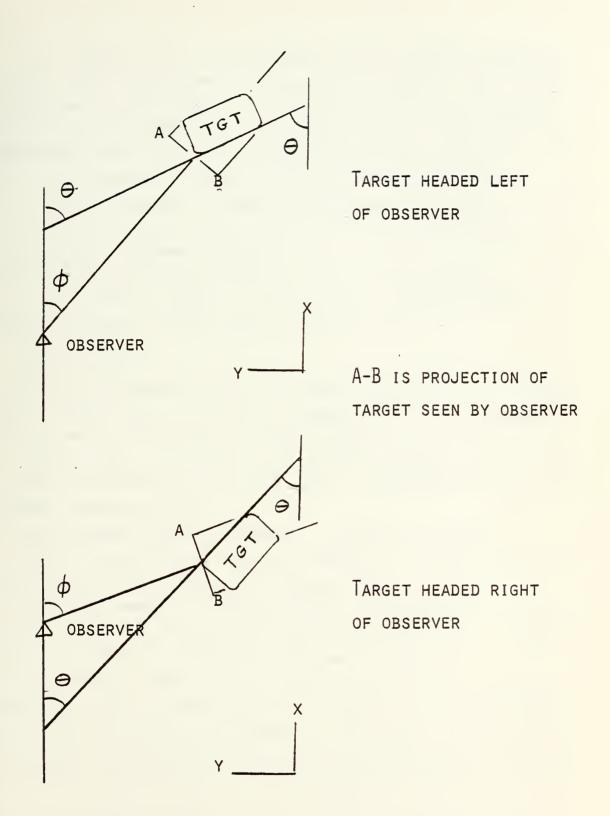


FIGURE 9: EFFECTIVE AREA OF TARGET

The output of the Movement/line-of-sight subroutine includes the elevation, coordinates, speed, per cent exposed, and area exposed at each one-second time increment. Additionally, a summary is provided at the end of the simulation. The information printed is listed below:

- 1. The number and length of intervisiblity segments.
- 2. Total distance traveled with intervisibility.
- 3. Total distance traveled without intervisibility.
- 4. Total distance traveled.
- 5. Average distance traveled with intervisibility.
- 6. Per cent of time in which intervisibility existed.
 Refer to Figures 15 and 16 for sample output.

B. A TEST CASE

Although numerous test runs were conducted, a single random sample was initially chosen so that an evaluation could be made of the model's usefulness in a real situation. The intent was to conduct the test in a manner similar to the actual projected use of the model. In this regard, the following steps occurred:

- 1. The military analyst selected a "type" of terrain.
- 2. The user applied the terrain description to the model by adjusting the input parameters (Figure 10).
- 3. The user executed SIMTER without the MOVLOS subroutine in order to obtain a graphical representation of a single random realization of terrain (Figures 11 and 12).
- 4. The analyst selected a location for the defender (observer), and routes for the attacker. The routes were chosen based on military judgement. For this case routes were based on maximizing cover while attempting to maintain good visual surveillance of the battlefield (Figures 13 and 14).
- 5. The analyst provided maximum and minimum speeds for the attacker. For this run the minimum speed was two meters per second and the maximum speed was ten meters per second.

These speeds occurred at a 45 degree positive slope and a 45 degree negative slope, respectively. Since the relationship was linear, level terrain velocity was six meters per secon.

6. The user resubmitted the program, this time without creating graphics but including MOVLOS instead. The resulting output (Figures 15 and 16) compared logically with what appeared on the terrain maps.

VARIABLES INPUT EXPLANATION OF

Explanation of Input Variables

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Input Variables Values of

Input Data Figure 10:

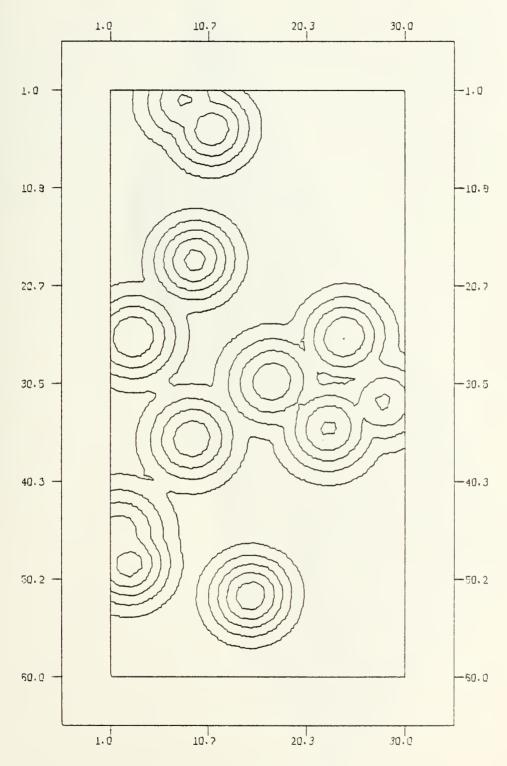
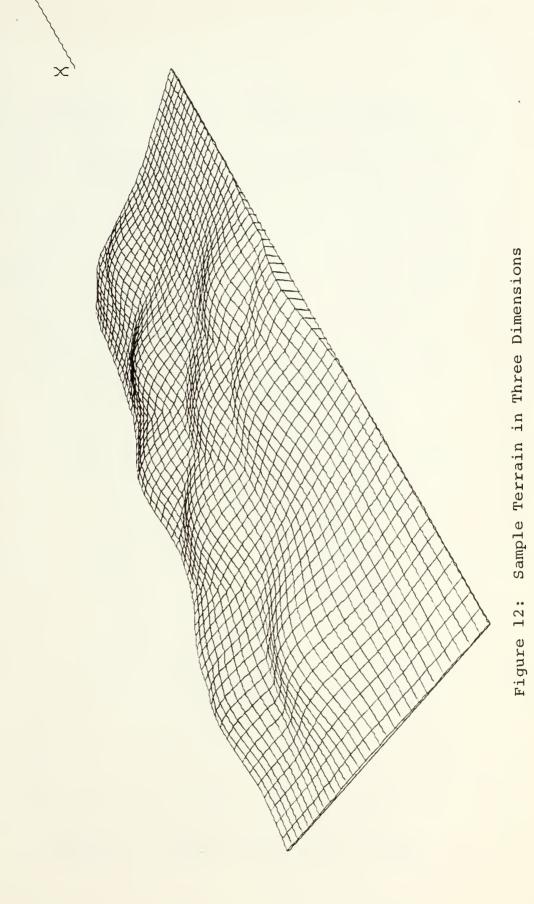


Figure 11: A Sample Terrain



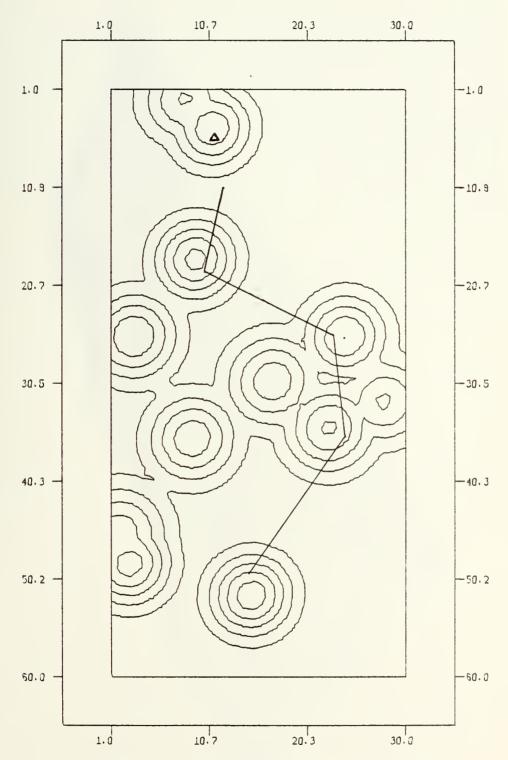


Figure 14: Sample Terrain with Routes

TERRAIN

Figure 14: Three Dimensional View of Routes

260.33130 270.45313 207.36163 251.57468 232.69176 242.16846 278.13281 249.65480 238.52051 208.90152	2146.65479 832.37500 731.26050 73.84763 999.23706 181.90198 226.73892 802.86084 2686.08423 2686.08423	3397.61450 1708.57959 100.46304 2482.80200 4456.73438 394.04761 4764.23047 2482.03125 3506.22534 3132.94922 400.00000 1010.0
278.13281 249.65480	181,90198	64.23047
242.16846	999.23706	94.04761
232.69176	79.84763	56.73438
251.57468	2299.93896	82.80200
207,36163	731.26050	00.46304
270.45313	832,37500	08.57959
260.33130	2146.65479	97.61450
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OF MOUNTAINS AND ELEVATIONS AT PEAKS 1591.02612

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Figure 16: Sample Output Data Continued

C. VERIFICATION

To ensure that the model was responding to all changes in parameters, a series of verification runs were conducted. It was not the intent of these replications to establish the sensitivity of line-of-sight to variations in terrain. The latter was the subject of the previously mentioned VRI study.

The first series of runs consisted of varying the number of hills (5,25, and 25) and the height of the hills (100,200,and 300). Since the same random number generator seeds were used for all nine runs, the 15 hills included the original 5, and the 25 hills included the original 15. This made it possible to use the same routes for all replications without violating tactical doctrine (Appendix D). A matrix of the results is presented in Table 1.

A second group of tests was conducted by varying the maximum and minimum speeds of the attacker over the same range of slopes (-45,+45). The initial (2,10) meters per second was run against (4,16) meters per second. The results yielded no significant difference between the two runs except that the faster target was intervisible 95 out of 501 seconds while the slower was intervisible 160 out of 836 seconds (both 19%).

AVERAGE ELEVATION OF TERRAIN PEAKS

a	sible									
Average Distance	Intervisible	2678	5370	2180	802	741	471	365	415	245
200 Number of Intervisible	Segments	2	_	က	ო	m	8	_	_	က
% Distance Uncovered		87.2	100.0	92.1	38.7	41.5	20.2	5.8	8.6	9.01
Route		V	മ	٥	A	83	U	A	В	O
Average Distance	Intervisible	2630	5370	3271	768	3471	1,1,38	370	416	269
100 Number of Intervisible	Segments	7	_	2	m	_	2	_	_	က
% Distance Uncovered		86.5	100.0	92.6	37.8	64.8	32.5	5.9	8.2	11.5
Route	c	⋖	മ	S	A	8	U	A	В	O
			വ			15			25	

Results of Varying Number of Hills and Elevation of Peaks Table 1:

NUMBER OF TERRAIN FEATURES

A third series of runs consisted of varying the spread of the hills in the initial test case, while holding all other parameters constant. As was expected, intervisibility decreased as the hills were widened.

SPREAD	PER CENT INTERVISIBLE
300	27.0
400	19.4
500	7.7

Table 2: Effect of Varying Spread on Intervisibilty

Other runs, such as varying the location (seeds) of the hills while holding routes constant, were executed but not included in this report.

VI. CONCLUSIONS

If exact terrain modelling is not required in a combat simulation, them representative terrain can be created using a modified bivariate normal distribution. Since there is no requirement for survey or photographic interpretation in order to mathematically model terrain, this approach is significantly less costly and time consuming than digitizing terrain. additional An advantage of mathematical representation is that replications of a "type" of terrain can be randomized, thereby improving the statistical of confidence in a combat model output.

The parameterized terrain is continuous; therefore, the elevation at any location is exact and not a linear interpolation between discrete points. This makes it possible for line-of-sight calculations to be more accurate. On the other hand if the program is to be used as a terrain preprocessor for a high resolution combat model, then SIMTER can produce a digitized output from the parameterized representation.

The results of the tests indicate that the parametric representation of terrain is both useful and realistic. In view of these conclusions the following action is recommended:

- 1. Parameterized terrain should be run against digitized actual terrain in a high resolution model such as DYNTACS or AMC 74. Sufficient replications of the randomized parametric terrain should be conducted in order to establish steady state results.
- 2. Distributions other than the bivariate normal should be examined, e.g. the beta.
- 3. The feasibility of representing actual terrain with the MBVN should be examined by preselecting centers of hills as they appear on a map.

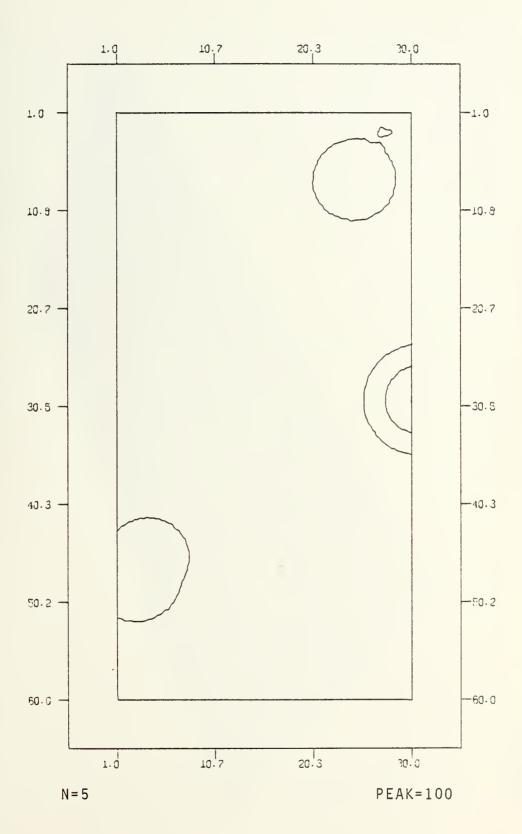
4. The SIMTER simulation should be evaluated for use as a mobility model. Routes can be selected or readily changed commensurate with vehicle performance.

APPENDIX A

MATRIX OF INPUT VARIABLES

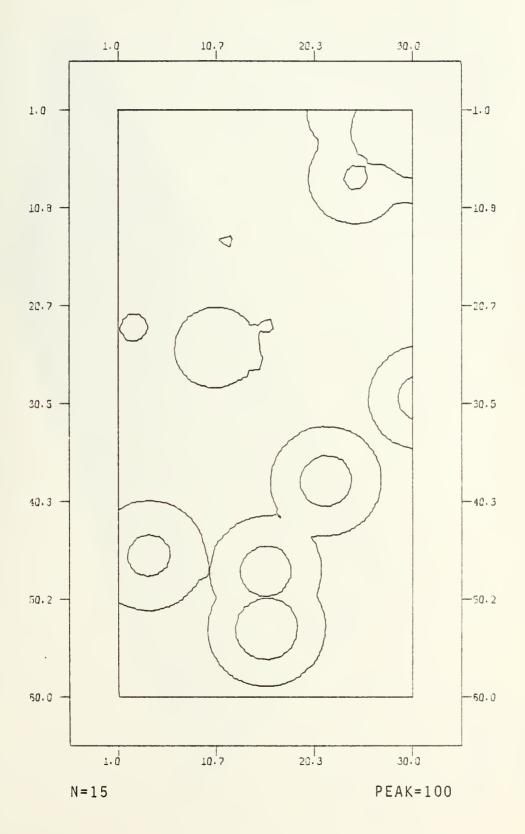
The graphs included in this appendix illustrate variations in number of terrain features (N) and average height of hills (PEAK). The graphs are presented in pairs; the first being the contour map and the second being its three dimensional representation. The order of variation is listed below.

N	PEAK
5	100
15	100
25	100
5	200
15	200
25	200
5	300
15	300
25	300

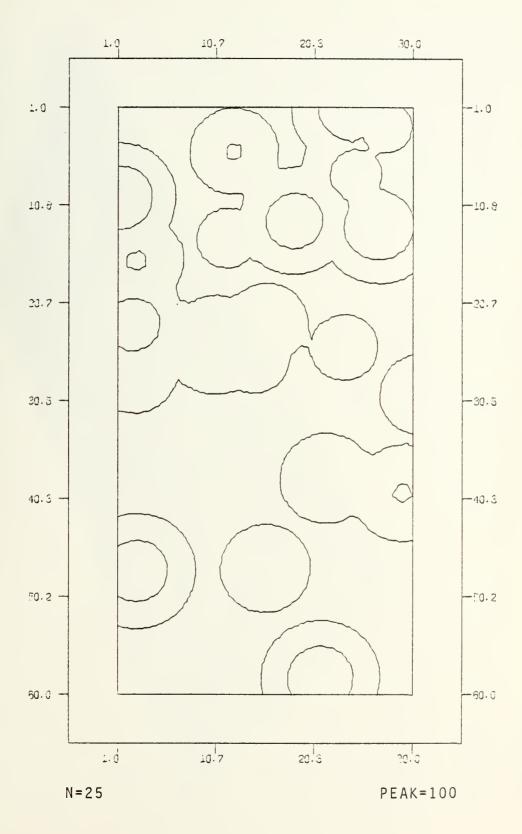


TERRAIN

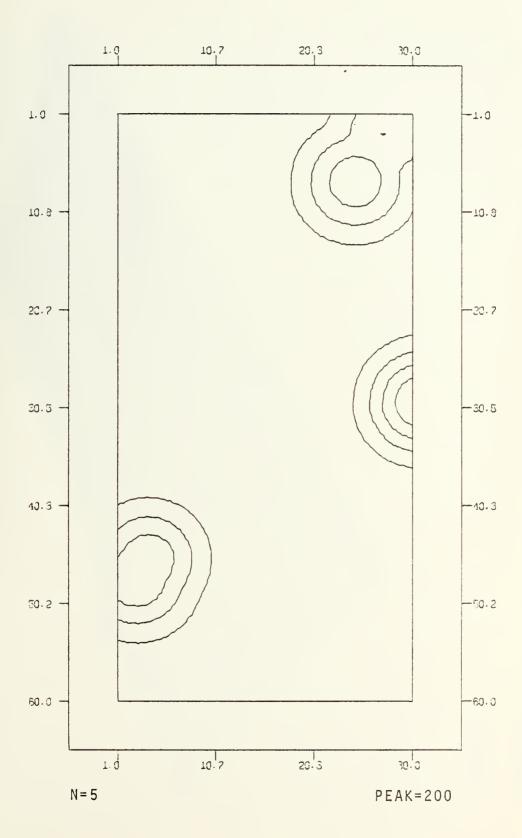
NEFDELS



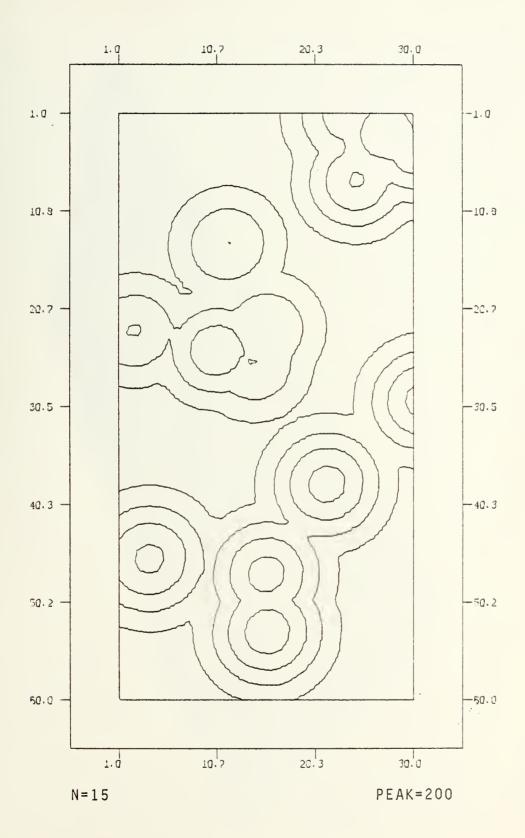
TERRAIN

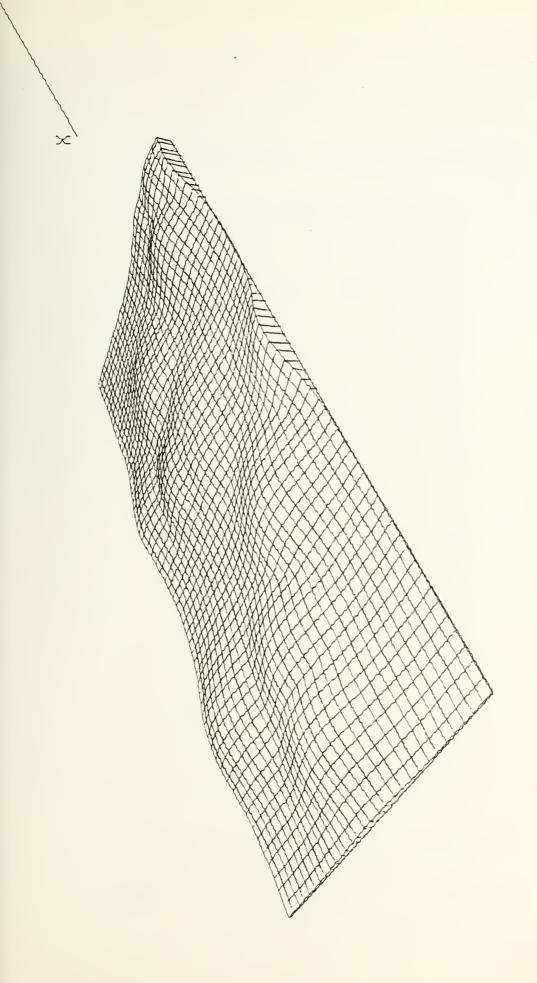


NEEDELS

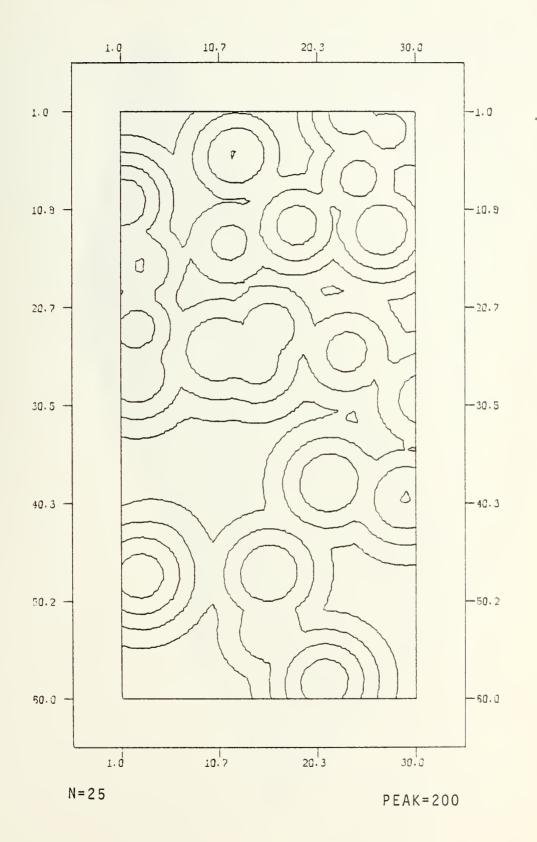


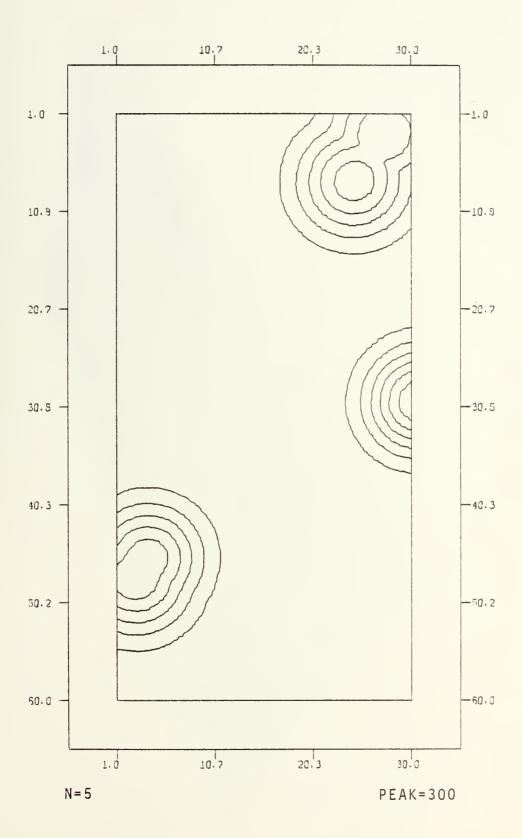
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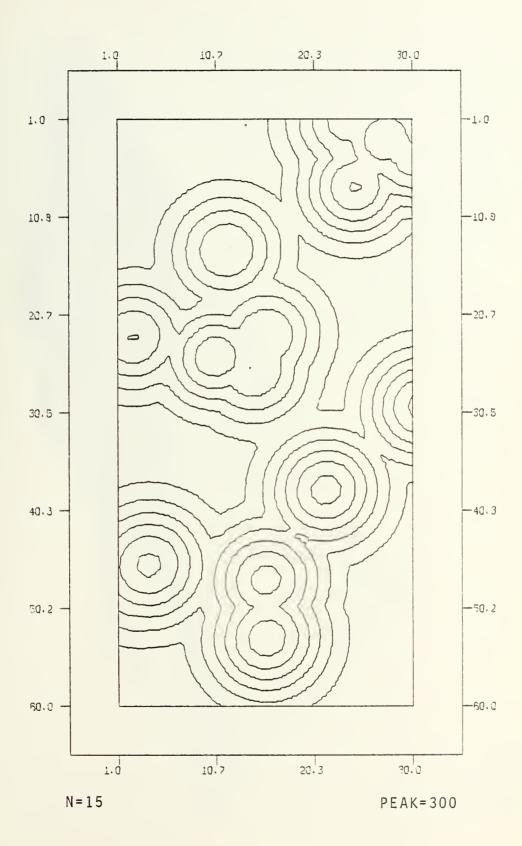


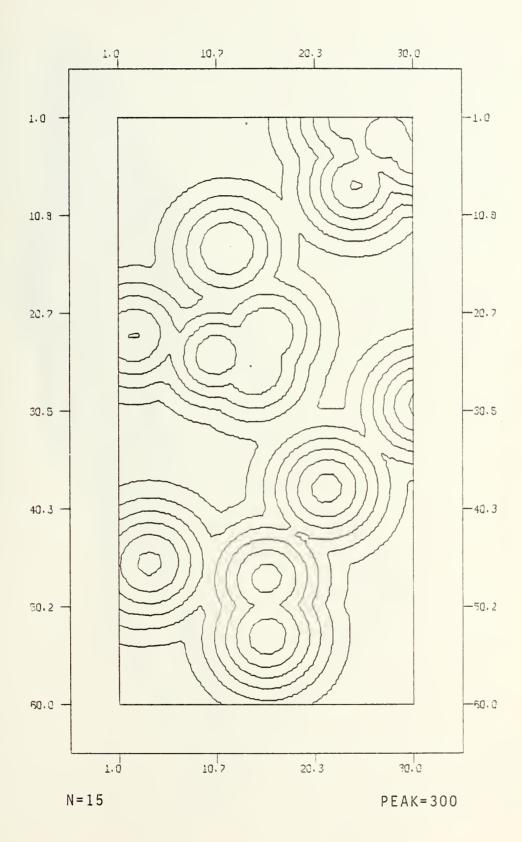
TERRAIN



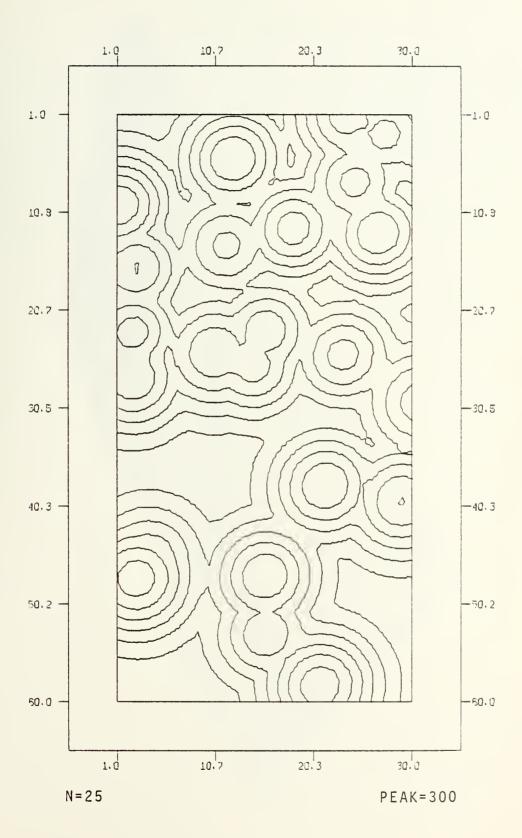


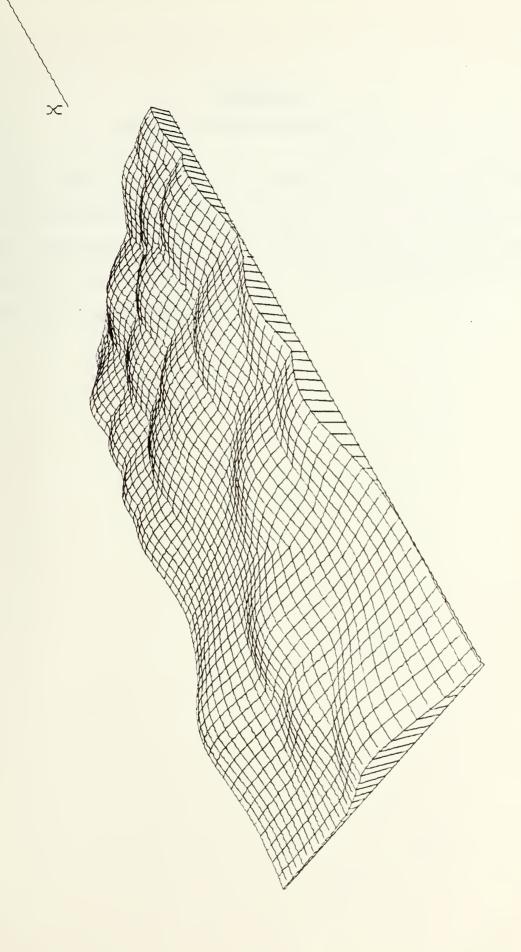
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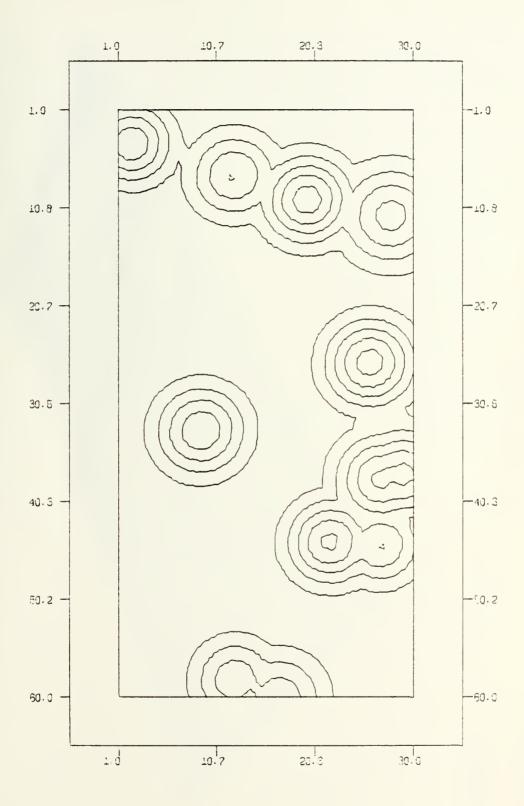




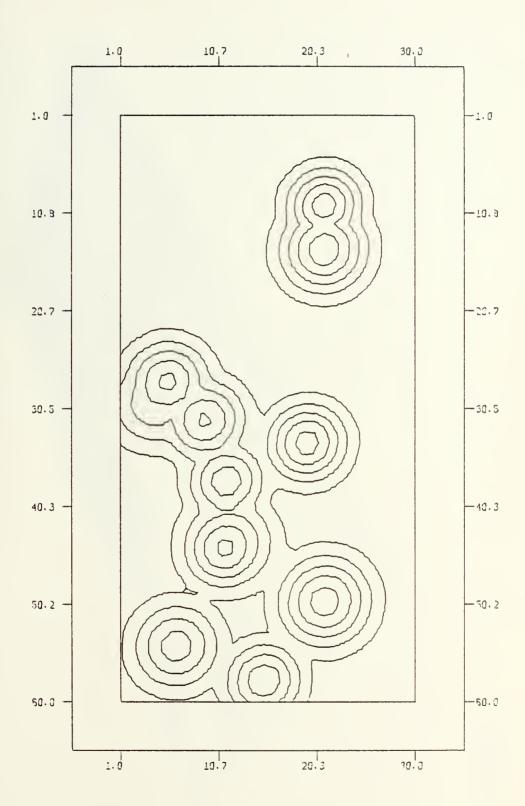
APPENDIX B

VARIABLE RANDOM NUMBER SEEDS

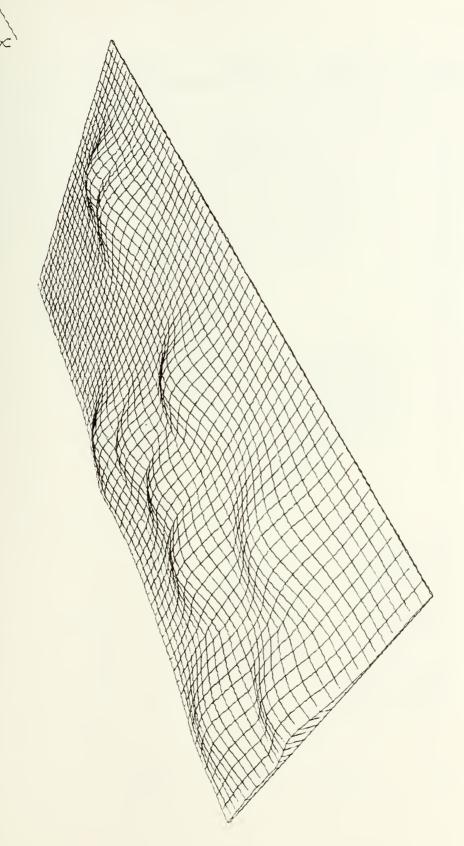
The graphs included in this appendix have the same constant input parameters. The only variable is the seed for the random number generator. As with the previous appendix, the graphs appear in pairs; the contour map first, followed by its three dimensional representation.

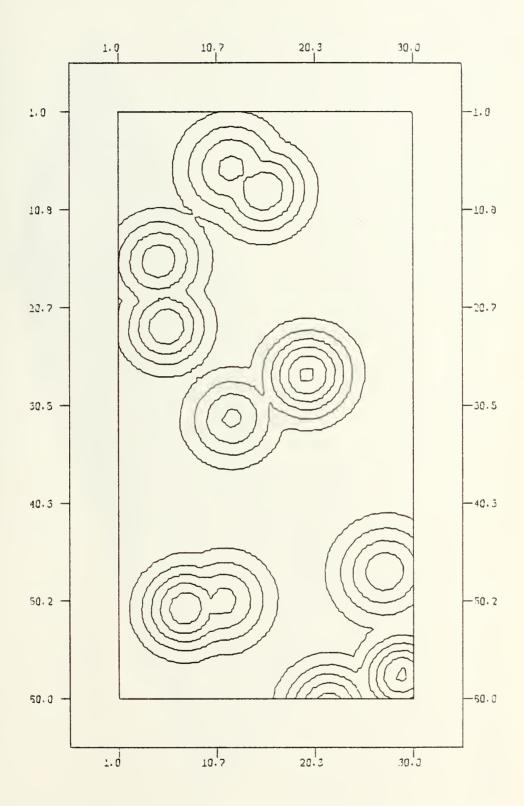


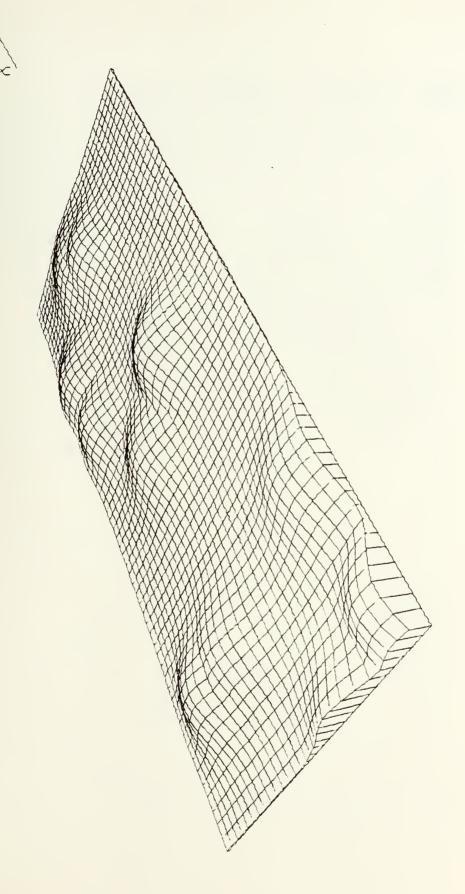
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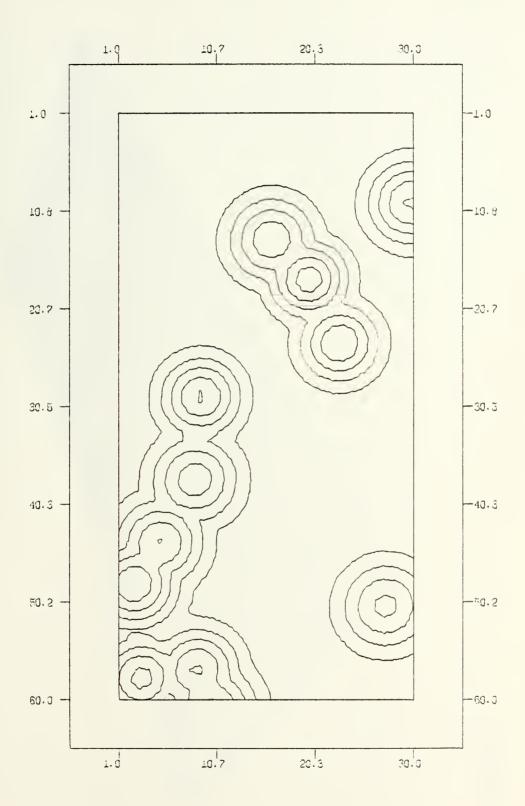
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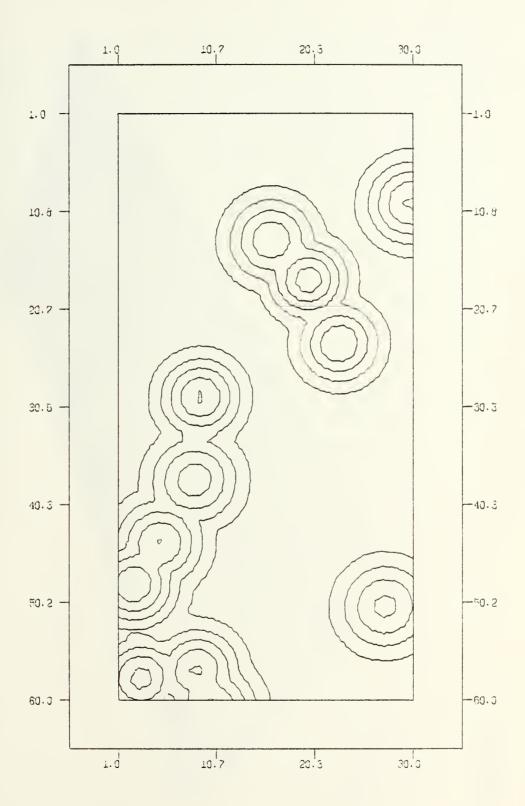


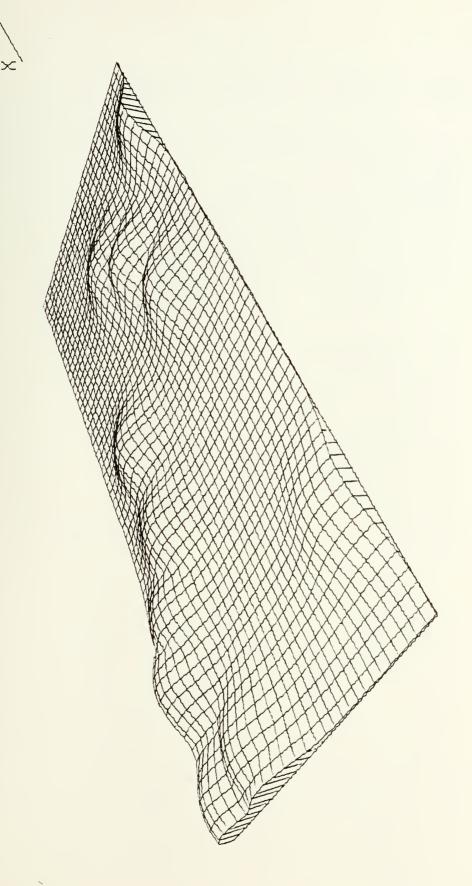




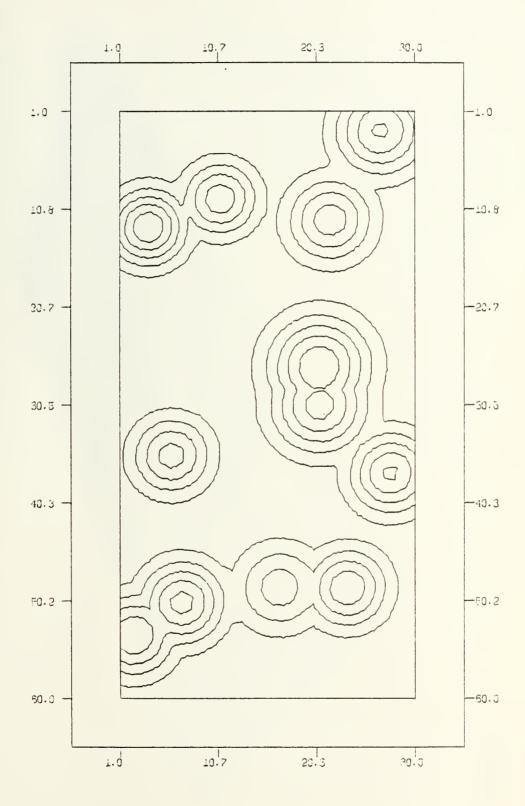
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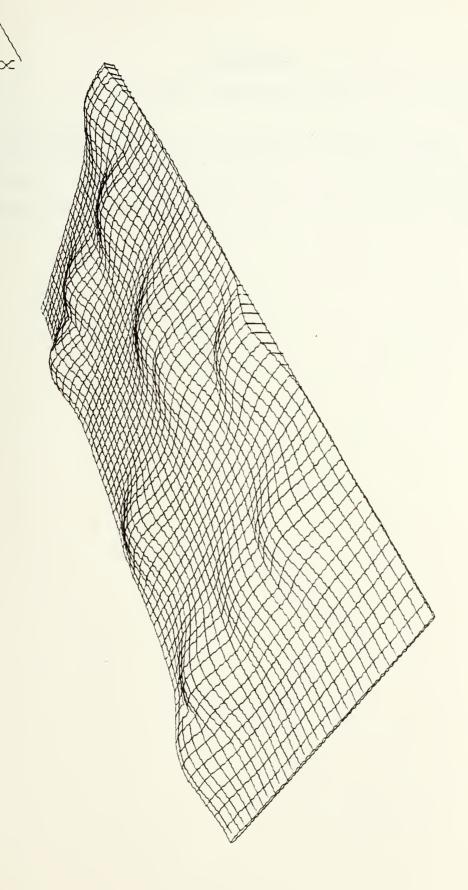




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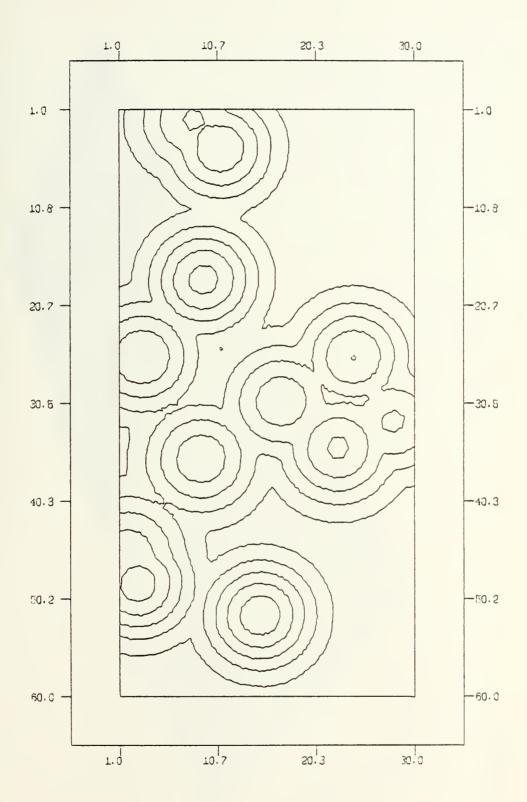
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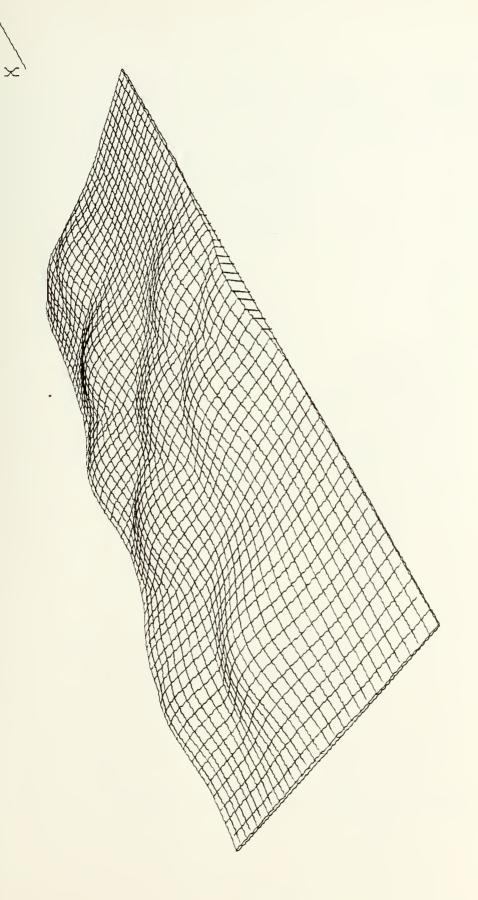
APPENDIX C

VARIABLE SPREAD OF HILLS

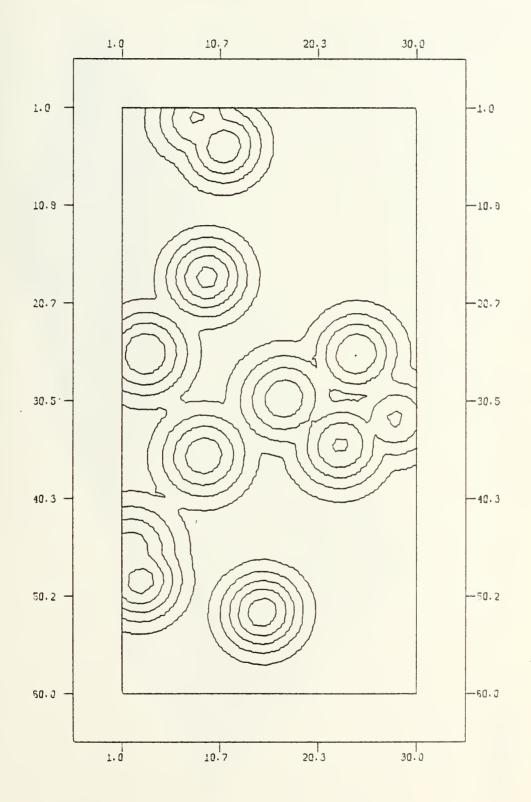
The graphs presented in Appendix C have constant input parameters except for the spread of the hills (XMEL, YMEL).

The three variations are 100,200, and 300 meters, respectively.

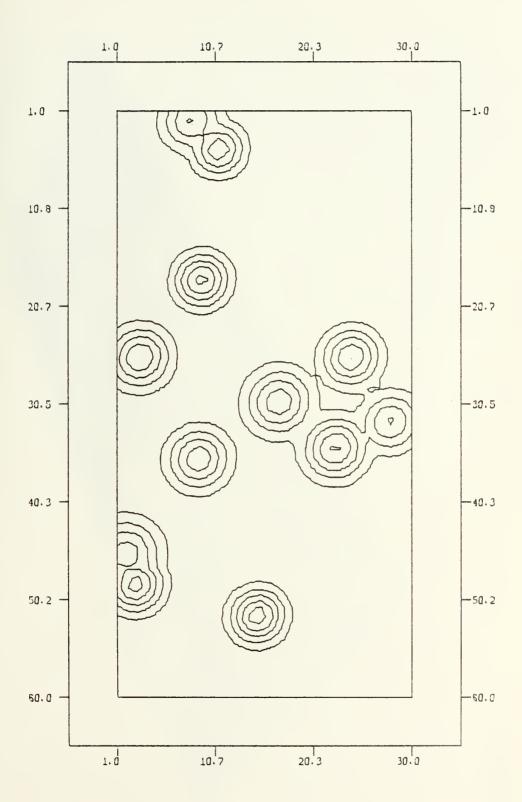




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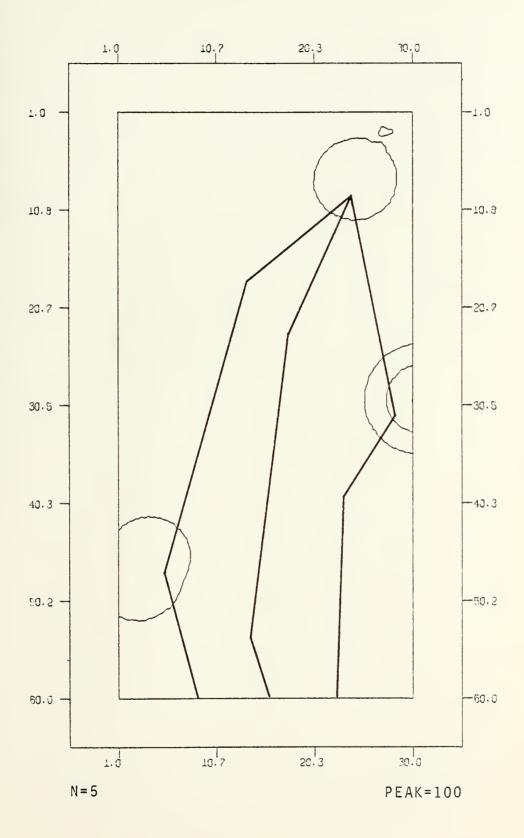
TERRAIN

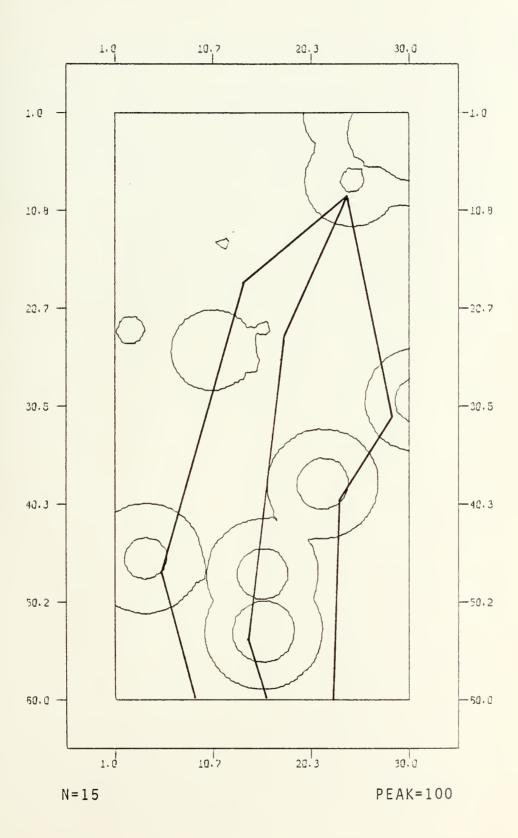
NEFDELS

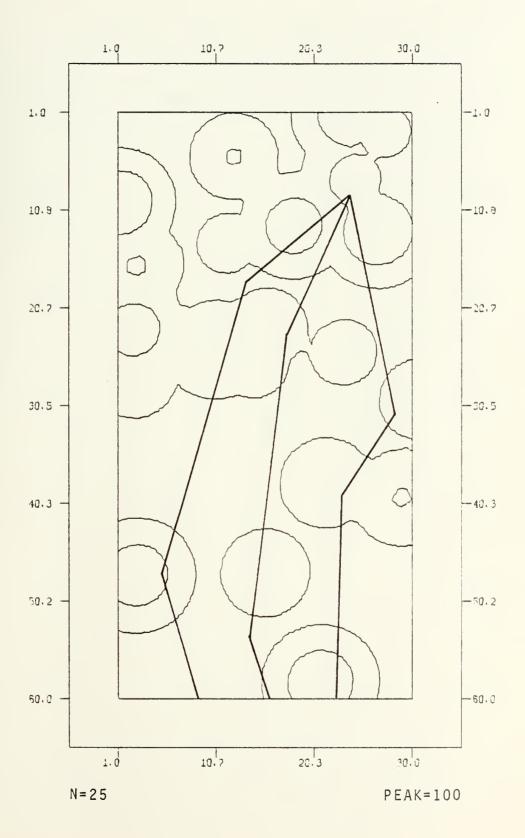
APPENDIX D

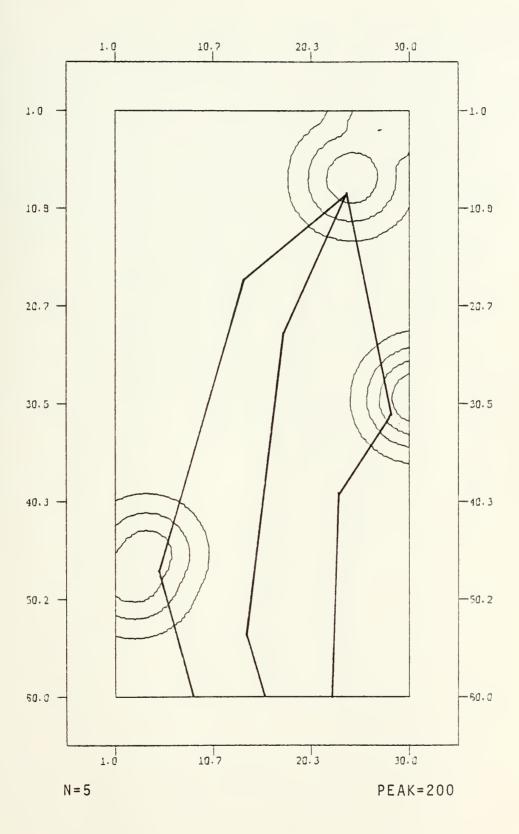
ROUTE SELECTION

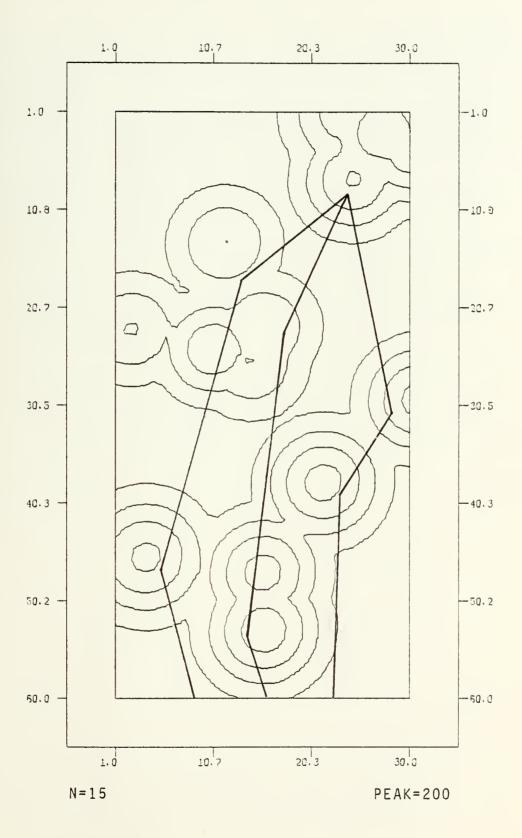
The contour maps in Appendix D are the same as those in Appendix A except for the overlayed routes. These graphs were used to develop input data for the line-of-sight subroutine.

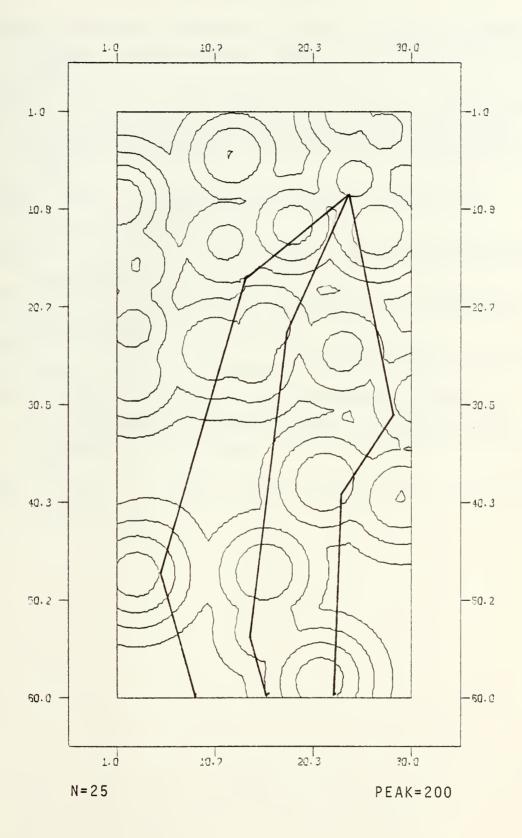












BIBLIOGRAPHY

- Bishop, Albert B., and Clark, Gordon M., <u>The Tank Weapon</u>

 <u>System</u>, Systems Research Group, Ohio State University,

 1969.
- Farrell, Robert L., and Freedman, Richard J., <u>Investigation</u>
 of the <u>Variation of Combat Model Predictions with</u>
 <u>Terrain Line F Sight</u>, Vector Research, Incorporated,
 1975.
- Graves, James W., <u>Tank Exchange Model</u>, Insitute for Defense Analyses, 1973.
- Luenberger, David G., <u>Introduction</u> to <u>Linear</u> and <u>Nonlinear</u>

 <u>Programming</u>, Addison-Wesley, 1973.
- Meyer, Paul L., <u>Introductory Probability and Statistical</u>
 Applications, Addison-Wesley, 1972.
- Murphy, N. R., and Alvium, R. B., AMC-74 Vehicle Dynamics
 Module, Waterways Experiment Station, 1976.
- Raney, Sharon D., <u>PLT3D1: Three Dimensional Isometric</u>
 or <u>Perspective Off-line Plotting Sub-program with</u>
 <u>Hidden-line Elimination</u>, Naval Postgraduate School,
 1974.
- Weir, Maurice D., <u>Topics in Calculus Two</u>, Naval Postgraduate School, 1973.

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